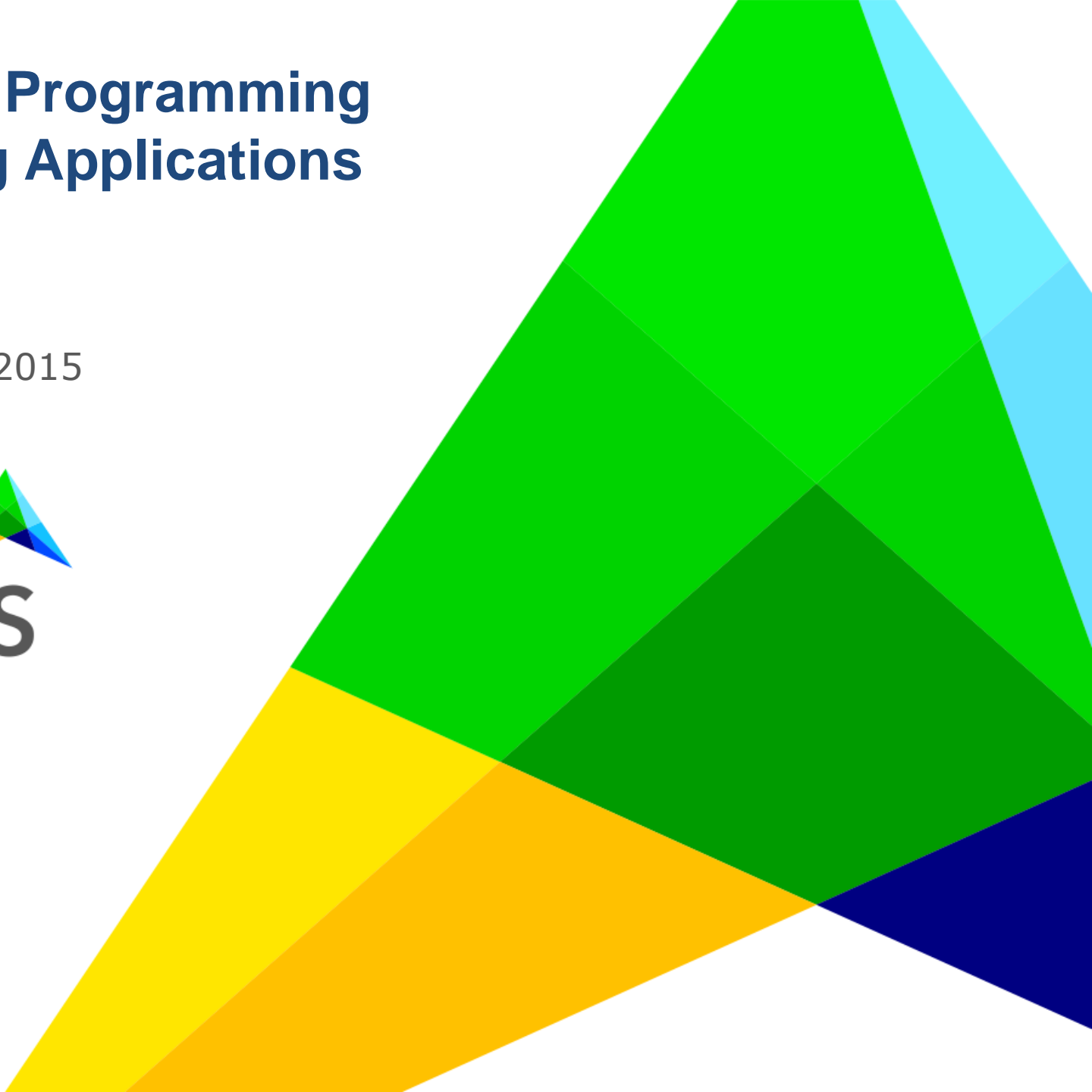


# Constraint Programming Scheduling Applications

Chris Kuip  
September 16, 2015



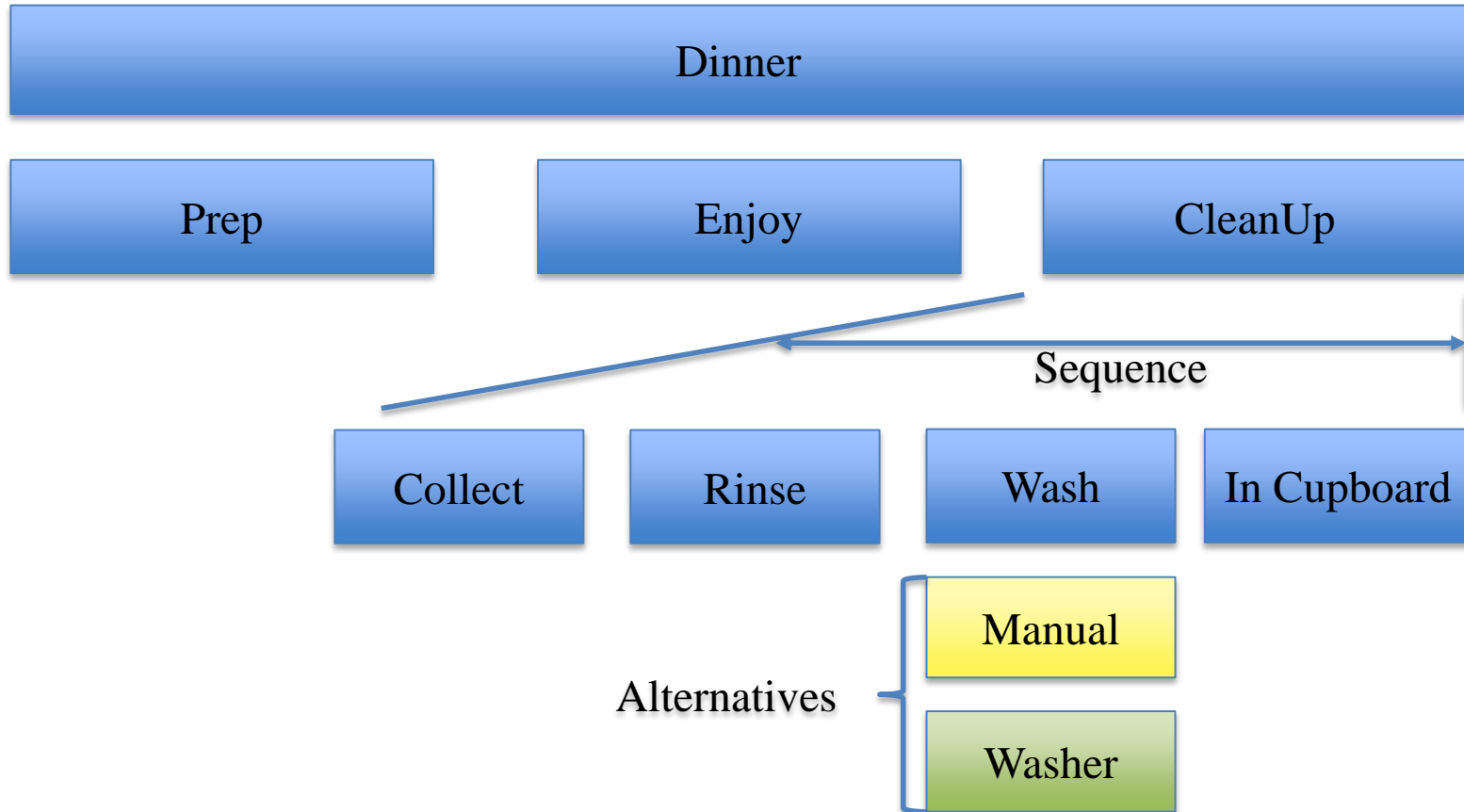
**AIMMS**



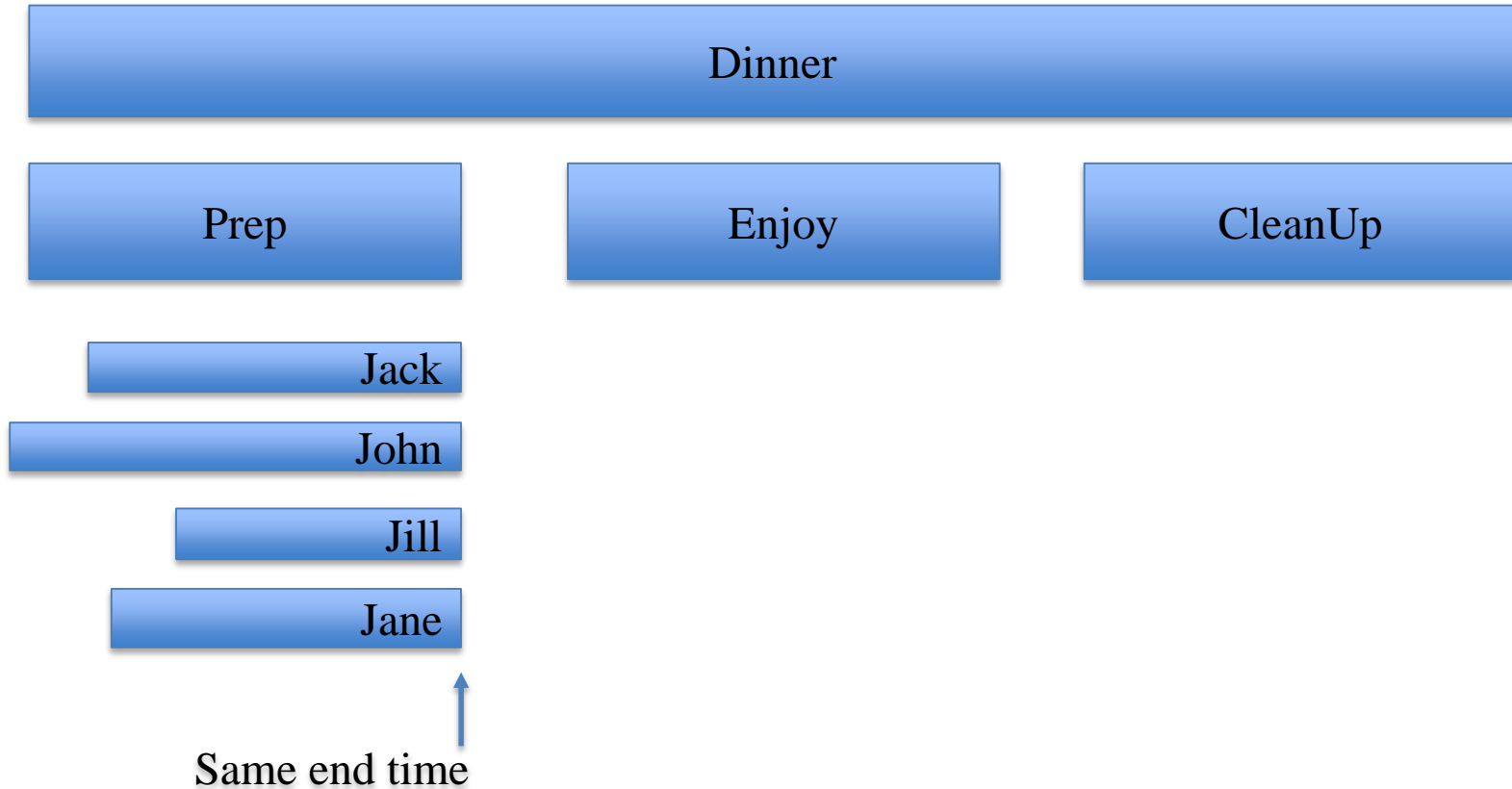
# Contents

- Introduction to Scheduling with Constraint Programming
- Maintenance scheduling
- Bridge building

# Trivial example: Dinner – Looking to CleanUp



# Trivial example: Dinner – Looking at preparation



# IBM/ILOG CP Optimizer technology used

- Special modeling constructs for scheduling
- Many years of research on algorithm development

# Overview AIMMS scheduling support

## 1. Mathematical Program

We start with establishing a timeline (scheduleDomain):

- Contiguous subset of Integers
- Calendar, or a contiguous subset thereof

Specified in the Mathematical Program, example:

```
MathematicalProgram findSchedule {  
    ...  
    ScheduleDomain: Ca_Quarters;  
}
```

# Overview AIMMS scheduling support

## 2. Activities A. Declaration.

Declaring activities:

1. Which activities are there?

- indexDomain: (i,j,...) | condition(i,j,...)
- Property: Optional

2. What do we know about these activities?

- scheduleDomain attribute, for instance:
  - A. timeline
  - B. { startTimeWindow .. endTimeWindow }
- Length(and perhaps size), defining constraint, for instance:
  - A. 5
  - B. 3 \* requiredNumberUnitsCreated

# Overview AIMMS scheduling support

## 2. Activities B. Suffices and simple constraints

An activity A consists of 5 integer variables represented by suffices:

- A.begin
- A.end
- A.length and A.size
- A.present

These suffices can be used to set up simple constraints such as:

DinnerPrep.End  $\leq$  DinnerEnjoy.begin ! Cook before enjoy.

DinnerPrep.End = DinnerPrepPerson(p).end ! Dinner is ready!

An activity A is active from A.begin  
up to but NOT including A.end

Notation: [A.begin, A.end)

Constraint that is implicitly enforced on every activity A:

If A.Present Then

    A.end = A.Begin + A.Length

Endif



# Overview AIMMS scheduling support

## 3. Precedence constraints

Relate two activities on `.begin`, `.end` and using `'='` or `'<='`

```
CP::EndBeforeBegin (prep, enjoy) ;
```

Equivalent to:

```
If prep.present and enjoy.present then
```

```
    prep.end <= enjoy.begin
```

```
Endif ;
```

The filtering for these precedence constraints is highly effective.

```
CP::BeginAtBegin(a,b,d)
```

```
CP::BeginAtEnd(a,b,d)
```

```
CP::EndAtBegin(a,b,d)
```

```
CP::EndAtEnd(a,b,d)
```

```
CP::BeginBeforeBegin(a,b,d)
```

```
CP::BeginBeforeEnd(a,b,d)
```

```
CP::EndBeforeBegin(a,b,d)
```

```
CP::EndBeforeEnd(a,b,d)
```

Only constrain if activities a and b are both present.

# Overview AIMMS scheduling support

## 4. Scheduling constraints

- An activity consists of several sub-activities

`cp::Span( g, i, a(i) )`

- There are several alternative ways to realize an activity

`cp::Alternative( g, i, a(i) )`

- Several activities need to take place at the same time:

`cp::Synchronize( g, i, a(i) )`

Only constrain if activities g and a(i) are present.

# Overview AIMMS scheduling support

## 5. Sequential resources

Resources that handle only one activity at a time.

Mandatory Attributes:

- scheduleDomain: timeline
- Activities: ajob, bjob(i), cjob(i,j)|allowedJob(i,j)

Optional Attributes:

- indexDomain: (i,j,...) | condition(i,j,...)

Optional attributes particular to sequential resources

- Transition: (job(i),job(j)) : times(i,j)
- firstActivity: ajob
- lastActivity: bjob('John')
- comesBefore: (ajob, bjob) ! Directly before
- precedes: (ajob,bjob) ! Somewhere before

# Demo Maintenance Scheduling

This app:

- One maintenance group available for maintenance
- Large tasks - large time window
- Small tasks - small time window

# Overview AIMMS scheduling support

## 6. Parallel resources a. Declaration

Resources that handle multiple activities at a time.

Mandatory Attributes:

- scheduleDomain: timeline
- Activities: ajob, bjob(i), cjob(i,j)|allowedJob(i,j)

Optional Attributes:

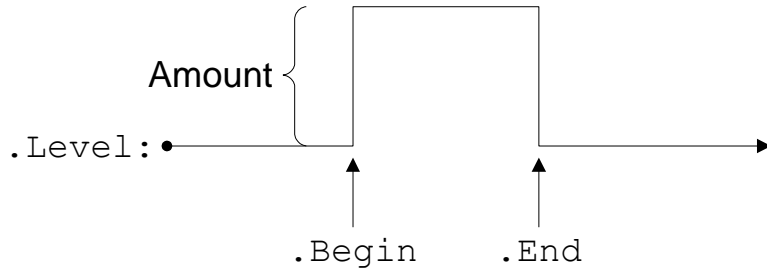
- indexDomain: (i,j,...) | condition(i,j,...)

Attributes particular to parallel resources

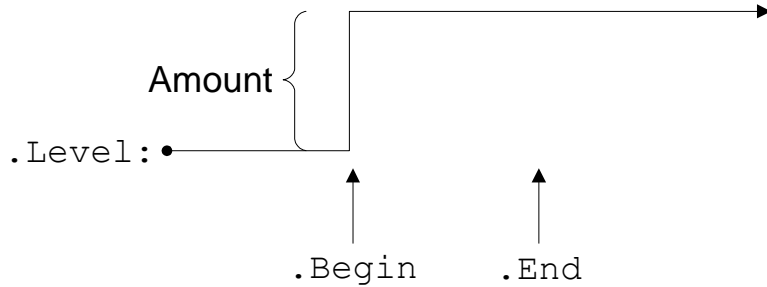
- levelRange: {0..pNumberOfShips}
- initialLevel: ajob
- levelChange: ajob : 1
- beginChange: bjob(i) : 1
- endChange: cjob(i,j): 2

# Overview AIMMS scheduling support

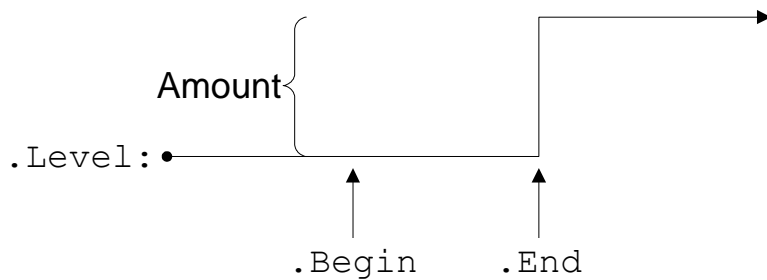
## 6. Parallel resources b. Pulses



Level change  
or pulse



Begin change



End change

# Overview AIMMS scheduling support

## 7. Difference .length and .size

Activities and resources may not be available every time slot.

For instance, human workers prefer to have weekends off.

Length does not suffice to measure amount of work done.

An activity A is active on timeslot t if

t is in scheduleDomain of A

And

t is in scheduleDomain of resource R,  
for every R on which A is scheduled.

For every activity A, we define A.size as  
the number of active timeslots in the range [A.begin,A.end)

Implicit constraint:

If a.present then

a.size <= a.length

Endif

# Demo Bridge Building

Build a bridge

- several components to be placed,
- several tools to be used.

Interesting:

- Activity
- Constraint
- Parallel Resource
- Gantt Chart



# Next webinar

- ?.
- ?
- October 2015

# Questions?

# Scheduling example

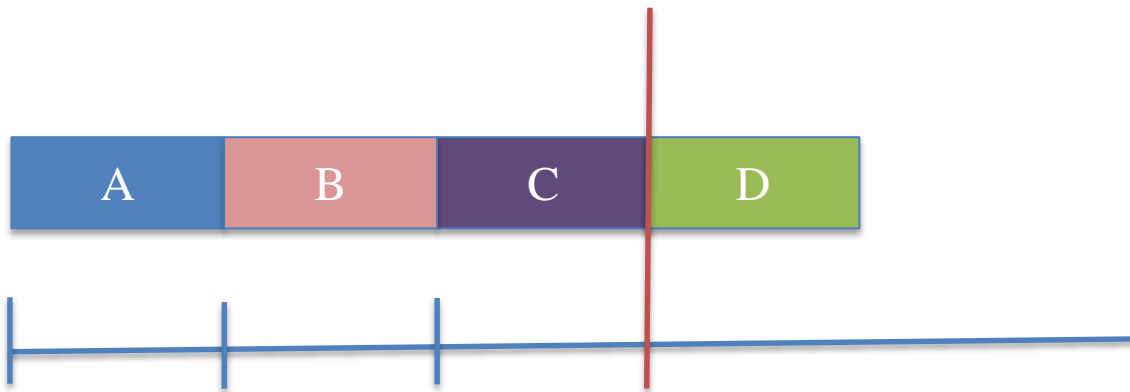
4 non overlapping activities A, B, C, D; each length 1, D comes last

Precedes(A, D)

Precedes(B, D)

Precedes(C, D)

NoOverlap(A,B,C,D)



From the above, scheduling engines can conclude begin of D  $\geq 3$ .

# Introduction to sequential resources

- Purpose: Scheduling sequences of activities
- Example:

```
Resource res {  
    Usage: sequential;  
    ScheduleDomain: TimeLine;  
    Activities: Act(j);  
    Transition: (act(j), act(k)) : ChgOver(j, k);  
}
```